

# Astronomer

Problem ID: astronomer

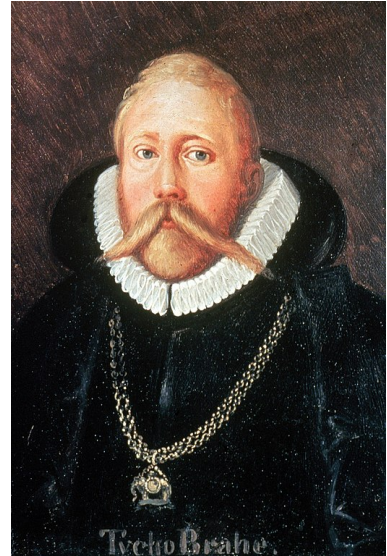
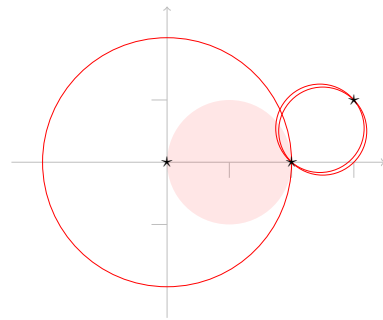
The astronomer has a passion for stargazing. In particular, he gets immense pleasure out of gazing at  $k$  stars simultaneously through his telescope. Building a telescope with radius  $r$  costs  $t \cdot r$  kroner. A newly built telescope will point exactly at the origin  $(0, 0)$ . Moving it to point somewhere else also takes effort; shifting the telescope a distance of  $d$  units incurs a cost of  $s \cdot d$  kroner. The astronomer can observe all stars at distance at most  $r$  from where the telescope points.

How much does it cost to build and move a telescope that allows  $k$  stars to be observed at once?

All coordinates and distances are given in the Euclidean plane.

## Example

Here is an example with  $n = 3$  stars at positions  $(0, 0)$ ,  $(2, 0)$ , and  $(3, 1)$ . The shaded area shows a telescope of radius 1 pointing at  $(1, 0)$  covering two stars; this costs  $s + t$  kroner and is an optimal solution to sample input 3. The image also shows optimal solutions to sample inputs 1, 2, and 4.



## Input

The first line consists of four integers: the number  $k$  of stars the astronomer wants to observe, the number  $n$  of stars in tonight's sky, the shifting cost  $s$ , and the telescope building cost  $t$ . Then follow  $n$  lines, where the  $i$ th line contains the integer coordinates  $x_i$  and  $y_i$  of the  $i$ th star.

## Output

A single real number: the minimum number of kroner that the astronomer needs to spend.

## Constraints and Scoring

You can assume

1.  $1 \leq k \leq n \leq 700$ .
2.  $x_i, y_i \in \{-10^9, \dots, 10^9\}$  for all  $i \in \{1, \dots, n\}$ .
3.  $s, t \in \{0, \dots, 10^9\}$ .
4. Your output is accepted if it is within a relative or absolute tolerance of  $\epsilon = 10^{-6}$  of the correct answer.

Your solution will be tested on a set of test groups, each worth a number of points. Each test group contains a set of test cases. To get the points for a test group you need to solve all test cases in the test group. Your final score will be the maximum score of a single submission.

Group	Points	Constraints
1	8	$t \leq s$
2	9	$n \leq 50$ and $s = 0$
3	18	$s = 0$
4	13	$n \leq 50$
5	14	$n \leq 350$
6	15	$\epsilon = 1/10$
7	23	<i>No further constraints</i>

#### Sample Input 1

```
2 3 1000 500
0 0
2 0
3 1
```

#### Sample Output 1

```
1000.0
```

#### Sample Input 2

```
2 3 500 3000
0 0
2 0
3 1
```

#### Sample Output 2

```
3387.277541898787
```

#### Sample Input 3

```
2 3 250 750
0 0
2 0
3 1
```

#### Sample Output 3

```
1000.0
```

#### Sample Input 4

```
2 3 0 500
0 0
2 0
3 1
```

#### Sample Output 4

```
353.5533905932738
```

#### Sample Input 5

```
3 4 0 10
0 0
10 0
5 10
5 5
```

#### Sample Output 5

```
50.0
```